

 **Learning Objective:** To solve equations with pronumerals and algebraic fractions.

Equations with Algebraic Fractions

To solve an equation that contains one fraction:

- Take all constant terms to one side by performing inverse operations
- Multiply both sides of the equation by the denominator
- Solve the resulting equation

Examples

Solve for x

$$\boxed{4 \times} \frac{2x+3}{4} = 2 \quad \boxed{\times 4}$$

$$2x+3=8$$

$$\boxed{-3} \quad \boxed{-3}$$

$$2x=5$$

$$\boxed{\div 2} \quad \boxed{\div 2}$$

$$\therefore x = \frac{5}{2}$$

Solve for t

$$\frac{3t}{2} - 4 = 2$$

$$\boxed{+4} \quad \boxed{+4}$$

$$\boxed{2 \times} \frac{3t}{2} = 6 \quad \boxed{\times 2}$$

$$3t = 12$$

$$\boxed{\div 3} \quad \boxed{\div 3}$$

$$\therefore t = 4$$

Solve for the pronumeral.

$$5h + 2 = 3h - 1$$

$$7 - 2h = 4h - 8$$

$$6h - 5 = 2 - 8h$$

$$4 - 2d = 7 - 3d$$

Solve for the pronumeral.

$$\frac{4t}{4} - 3 = 5$$

$$\frac{4t}{2} - 6 = 3$$

$$\frac{s}{2} - 6 = 1$$

$$\frac{2b}{3} - 3 = 7$$



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Solving One-step and Two-step Equations

To simplify an expression with grouping symbols:

- Expand the expression in grouping symbols by multiplying the term outside the grouping symbols by each term inside.
- Collect like terms if possible.

To solve a linear equation:

- Isolate the pronumeral by performing the inverse operation to both sides of the equation.

Example:

Simplify

$$\begin{aligned} 5(3a - 2) - 2a &= (5 \times 3a) + (5 \times -2) - 2a \\ &= (15a - 2a) - 10 \\ &= 13a - 10 \end{aligned}$$

Solve for x

$$\begin{aligned} 3x + 10 &= 22 \\ \boxed{-10} \quad \boxed{-10} \\ 3x &= 12 \\ \boxed{\div 3} \quad \boxed{\div 3} \\ \therefore x &= 4 \end{aligned}$$

Solve for y

$$\begin{aligned} 6 \times \frac{5y}{6} &= 10 \times 6 \\ 5y &= 60 \\ \boxed{\div 5} \quad \boxed{\div 5} \\ \therefore y &= 12 \end{aligned}$$

Solve for the pronumeral.

$$5h + 2 = 3h - 1$$

$$\begin{aligned} 5h + 2 &= 3h - 1 \\ 5h - 3h + 2 &= -1 \\ 2h &= -1 + 2 \\ 2h &= 1 \\ h &= 1/2 \\ h &= 0.5 \end{aligned}$$

$$7 - 2h = 4h - 8$$

$$\begin{aligned} 7 - 2h &= 4h - 8 \\ 7 + 8 - 2h &= 4h \\ 15 - 2h &= 4h \\ 15 &= 4h + 2h \\ 15 &= 6h \\ h &= 15/6 \\ h &= 5/2 \\ h &= 2.5 \end{aligned}$$

$$6h - 5 = 2 - 8h$$

$$\begin{aligned} 6h - 5 &= 2 - 8h \\ 6h + 8h - 5 &= 2 \\ 14h - 5 &= 2 \\ 14h &= 2 + 5 \\ 14h &= 7 \\ h &= 7/14 \\ h &= 0.5 \end{aligned}$$

$$4 - 2d = 7 - 3d$$

$$\begin{aligned} 4 - 2d &= 7 - 3d \\ 4 - 2d + 3d &= 7 \\ 4 + d &= 7 \\ d &= 7 - 4 \\ d &= 3 \end{aligned}$$

Solve for the pronumeral.

$$\frac{4t}{4} - 3 = 5$$

$$\begin{aligned} \frac{4t}{4} - 3 &= 5 \\ \frac{4t}{4} &= 5 + 3 \\ \frac{4t}{4} &= 8 \\ 4t &= 8 \times 4 \\ 4t &= 32 \\ t &= 32 / 4 \\ t &= 8 \end{aligned}$$

$$\frac{4t}{2} - 6 = 3$$

$$\begin{aligned} \frac{4t}{2} - 6 &= 3 \\ \frac{4t}{2} &= 3 + 6 \\ \frac{4t}{2} &= 9 \\ 4t &= 9 \times 2 \\ 4t &= 18 \\ t &= 18 / 4 \\ t &= 4.5 \end{aligned}$$

$$\frac{s}{2} - 6 = 1$$

$$\begin{aligned} \frac{s}{2} - 6 &= 1 \\ \frac{s}{2} &= 1 + 6 \\ \frac{s}{2} &= 7 \\ s &= 7 \times 2 \\ s &= 14 \end{aligned}$$

$$\frac{2b}{3} - 3 = 7$$

$$\begin{aligned} \frac{2b}{3} - 3 &= 7 \\ \frac{2b}{3} &= 7 + 3 \\ \frac{2b}{3} &= 10 \\ 2b &= 10 \times 3 \\ 2b &= 30 \\ b &= 30 / 2 \\ b &= 15 \end{aligned}$$