

 **Learning Objective:** To solve angles, triangles, and angle relationships.

### Quadrilaterals and Polygons

The sum of the exterior angles of any convex polygon is  $360^\circ$

In any regular  $n$  – sided convex polygon, each exterior angle measures:

$$\text{Exterior angles} = \frac{360^\circ}{n}$$

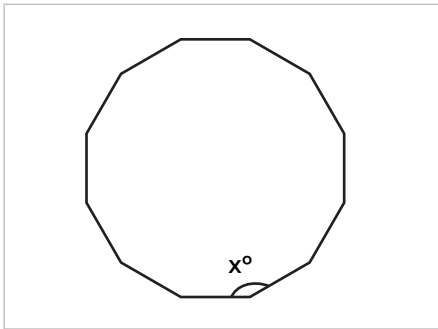
### Example

**Find the size of each exterior angle of a regular pentagon.**

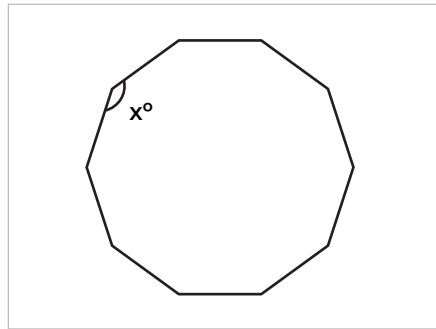
$$\begin{aligned} \text{Exterior angles} &= \frac{360^\circ}{n} \\ &= \frac{360^\circ}{5} \\ &= 72^\circ \end{aligned}$$

Therefore, each exterior angle is  $72^\circ$ .

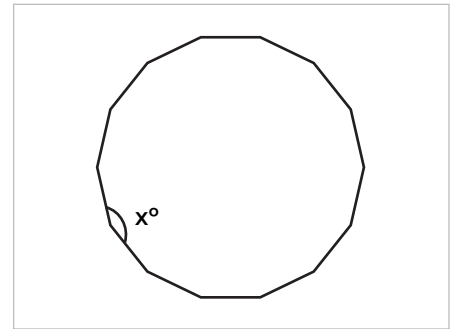
Find the angle sum of the regular polygon. Hence, find the value of  $x^\circ$




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How many sides are there in a regular polygon whose exterior angles each measure:

$12^\circ$

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$15^\circ$

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$30^\circ$

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$60^\circ$

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## Quadrilaterals and Polygons

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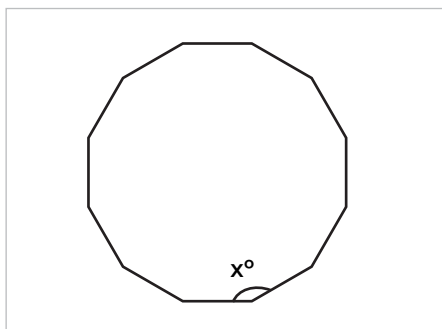
### Example

Find the size of each exterior angle of a regular pentagon.

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Therefore, each exterior angle is  $72^\circ$ .

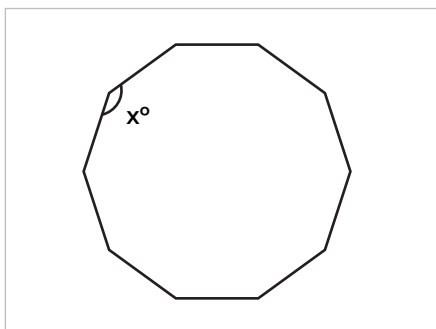
Find the angle sum of the regular polygon. Hence, find the value of  $x^\circ$  to the nearest degree.



$$\begin{aligned} S &= (n - 2) \times 180^\circ \\ &= (12 - 2) \times 180^\circ \\ &= 1800^\circ \end{aligned}$$

Since all angles are equal in a regular polygon,

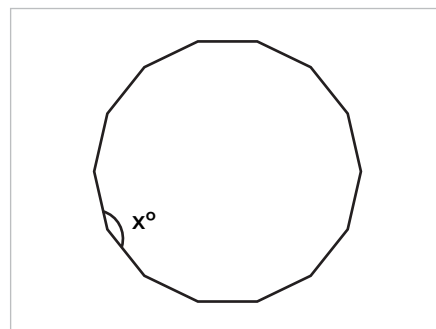
$$\begin{aligned} x^\circ &= 1800 / 12 \\ x^\circ &= 150^\circ \end{aligned}$$



$$\begin{aligned} S &= (n - 2) \times 180^\circ \\ &= (10 - 2) \times 180^\circ \\ &= 1440^\circ \end{aligned}$$

Since all angles are equal in a regular polygon,

$$\begin{aligned} x^\circ &= 1440 / 10 \\ x^\circ &= 144^\circ \end{aligned}$$



$$\begin{aligned} S &= (n - 2) \times 180^\circ \\ &= (14 - 2) \times 180^\circ \\ &= 2160^\circ \end{aligned}$$

Since all angles are equal in a regular polygon,

$$\begin{aligned} x^\circ &= 2160 / 14 \\ x^\circ &= 154^\circ \end{aligned}$$

How many sides are there in a regular polygon whose exterior angles each measure:

**12°**

$$\begin{aligned} \text{Exterior angles} &= 360^\circ / n \\ 12 &= 360^\circ / n \\ 12n &= 360 \\ n &= 360 / 12 \\ n &= 30 \end{aligned}$$

Therefore, the polygon has 30 sides.

**15°**

$$\begin{aligned} \text{Exterior angles} &= 360^\circ / n \\ 15 &= 360^\circ / n \\ 15n &= 360 \\ n &= 360 / 15 \\ n &= 24 \end{aligned}$$

Therefore, the polygon has 24 sides.

**30°**

$$\begin{aligned} \text{Exterior angles} &= 360^\circ / n \\ 30 &= 360^\circ / n \\ 30n &= 360 \\ n &= 360 / 30 \\ n &= 12 \end{aligned}$$

Therefore, the polygon has 12 sides.

**60°**

$$\begin{aligned} \text{Exterior angles} &= 360^\circ / n \\ 60 &= 360^\circ / n \\ 60n &= 360 \\ n &= 360 / 60 \\ n &= 6 \end{aligned}$$

Therefore, the polygon has 6 sides.