

 **Learning Objective:** Multiplication, division and negative index laws.

### Index Law for further powers:

$$(a^m)^n = a^{m \times n}$$

$$(a \times b)^m = a^m \times b^m$$

$$\left(\frac{a}{b}\right)^m = \frac{a^m}{b^m}$$

- Raise any coefficient to the power outside grouping symbols
- Keep the same base
- Multiply the indices

### Example:

Simplify

$$(a^4)^3 = a^{4 \times 3} = a^{12}$$

$$(5k)^2 = 5^2 k^2 = 25k^2$$

$$\left(\frac{2x^3}{y^5}\right)^6 = \frac{2^{1 \times 6} x^{3 \times 6}}{y^{5 \times 6}} = \frac{64x^{18}}{y^{30}}$$

Simplify the following questions.

$$(r^8)^8$$

$$(7l)^3$$

$$\left(\frac{3b^4}{7d^2}\right)^2$$

$$\left(\frac{6g^7}{5h^{11}}\right)^2$$

Simplify the following, giving answers without negative indices.

$$\frac{(x^{-3}y^5)^2}{x^3y^{-6}}$$

$$\frac{a^{-2}b^5}{(a^3b^{-2})^3}$$

$$\frac{(w^{-2}v^3)^2}{w^6v^{-2}}$$

$$\frac{d^{-3}e^7}{(d^5e^{-2})^3}$$



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Simplify the following questions.

$$(r^8)^8$$

$$\begin{aligned} (r^8)^8 &= r^{8 \times 8} \\ &= r^{64} \end{aligned}$$

$$(7l)^3$$

$$\begin{aligned} (7l)^3 &= 7^3 \times l^3 \\ &= 343l^3 \end{aligned}$$

$$\left(\frac{3b^4}{7d^2}\right)^2$$

$$\begin{aligned} \left(\frac{3b^4}{7d^2}\right)^2 &= \frac{3^2 b^{4 \times 2}}{7^2 d^{2 \times 2}} \\ &= \frac{9b^8}{49d^4} \end{aligned}$$

$$\left(\frac{6g^7}{5h^{11}}\right)^2$$

$$\begin{aligned} \left(\frac{6g^7}{5h^{11}}\right)^2 &= \frac{6^2 g^{7 \times 2}}{5^2 h^{11 \times 2}} \\ &= \frac{36g^{14}}{25h^{22}} \end{aligned}$$

Simplify the following, giving answers without negative indices.

$$\frac{(x^{-3}y^5)^2}{x^3y^{-6}}$$

$$\begin{aligned} \frac{(x^{-3}y^5)^2}{x^3y^{-6}} &= \frac{x^{-6}y^{10}}{x^3y^{-6}} \\ &= x^{-6-3} y^{10-(-6)} \\ &= x^{-9} y^{16} \\ &= \frac{y^{16}}{x^9} \end{aligned}$$

$$\frac{a^{-2}b^5}{(a^3b^{-2})^3}$$

$$\begin{aligned} \frac{a^{-2}b^5}{(a^3b^{-2})^3} &= \frac{a^{-2}b^5}{a^9b^{-6}} \\ &= a^{-2-9} b^{5-(-6)} \\ &= a^{-11} b^{11} \\ &= \frac{b^{11}}{a^{11}} \\ &= \left(\frac{b}{a}\right)^{11} \end{aligned}$$

$$\frac{(w^{-2}v^3)^2}{w^6v^{-2}}$$

$$\begin{aligned} \frac{(w^{-2}v^3)^2}{w^6v^{-2}} &= \frac{w^{-4}v^6}{w^6v^{-2}} \\ &= w^{(-4)-6} v^{6-(-2)} \\ &= w^{-10} v^8 \\ &= \frac{v^8}{w^{10}} \end{aligned}$$

$$\frac{d^{-3}e^7}{(d^5e^{-2})^3}$$

$$\begin{aligned} \frac{d^{-3}e^7}{(d^5e^{-2})^3} &= \frac{d^{-3}e^7}{d^{15}e^{-6}} \\ &= d^{-3-15} e^{7-(-6)} \\ &= d^{-18} e^{13} \\ &= \frac{e^{13}}{d^{18}} \end{aligned}$$