

MATHEMATICS: INDICES

## Index Law for further powers: **Example:** $\left(\frac{a}{b}\right)^m$ $a^m$ Simplify $(a^m)^n = a^{m \times n}$ $(a \times b)^m = a^m \times b^m$ $=\frac{a}{b^m}$ $\begin{array}{c|c} (a^4)^3 = a^{4\times 3} \\ = a^{12} \end{array} \begin{array}{c} (5k)^2 = 5^2 k^2 \\ = 25k^2 \end{array} \left( \frac{2x^3}{y^5} \right)^6 = \frac{2^{1\times 6} x^{3\times 6}}{y^{5\times 6}} \\ = \frac{64x^{18}}{y^{30}} \end{array} \right)$ Raise any coefficient to the power outside • grouping symbols Keep the same base • Multiply the indices . Simplify the following questions.

(m <sup>9</sup> )⁵	(5s) <sup>4</sup>	$\left(\frac{6b^2}{5d^3}\right)^3$	$\left(\frac{8g^6}{3h^9}\right)^2$

Simplify the following, giving answers without negative indices.

$\frac{(x^{-2}y^4)^2}{x^5y^{-7}}$	<u>a<sup>-3</sup>b<sup>6</sup></u> (a <sup>2</sup> b <sup>-4</sup> ) <sup>2</sup>	$\frac{(w^{-4}v^5)^2}{w^7v^{-4}}$	$\frac{d^{-5}e^{6}}{(d^{4}e^{-3})^{2}}$



## MATHEMATICS: ANSWER SHEET

**Learning Objective:** Multiplication, division and negative index laws.

## Index Law for further powers:Example: $(a^m)^n = a^{m \times n}$ $(a \times b)^m = a^m \times b^m$ $(\frac{a}{b})^m = \frac{a^m}{b^m}$ $\cdot$ Raise any coefficient to the power outside grouping symbolsSimplify $\cdot$ Keep the same base $(a^4)^3 = a^{4 \times 3}$ $(5k)^2 = 5^2k^2$ $(\frac{2x^3}{y^5})^6 = \frac{2^{1 \times 6}x^{3 \times 6}}{y^{5 \times 6}}$ $\cdot$ Multiply the indices

## Simplify the following questions.

(m <sup>9</sup> ) <sup>5</sup>	(5s) <sup>4</sup>	$\left(\frac{6b^2}{5d^3}\right)^3$	$\left(\frac{8g^6}{3h^9}\right)^2$
(m <sup>9</sup> ) <sup>5</sup> = m <sup>9×5</sup> = m <sup>45</sup>	$(5s)^4 = 5^4 \times s^4$ = 625d <sup>4</sup>	$\left(\frac{6b^2}{5d^3}\right)^3 = \frac{6^3b^{2\times 3}}{5^3d^{3\times 3}}$ $= \frac{216b^6}{125d^9}$	$\left(\frac{8g^{6}}{3h^{9}}\right)^{2} = \frac{8^{2}g^{6\times2}}{3^{2}h^{9\times2}}$ $= \frac{64g^{12}}{9h^{18}}$

Simplify the following, giving answers without negative indices.

$\frac{(x^{-2}y^4)^2}{x^5y^{-7}}$	<u>a<sup>-3</sup>b<sup>6</sup></u> (a <sup>2</sup> b <sup>-4</sup> ) <sup>2</sup>	$\frac{(w^{-4}v^{5})^{2}}{w^{7}v^{-4}}$	$\frac{d^{-5}e^{6}}{(d^{4}e^{-3})^{2}}$
$\frac{(x^{-2}y^{4})^{2}}{x^{5}y^{-7}} = \frac{x^{-4}y^{8}}{x^{5}y^{-7}}$ $= x^{-4} - 5y^{8} - (-7)$ $= x^{-9}y^{15}$ $= \frac{y^{15}}{x^{9}}$	$\frac{a^{-3}b^{6}}{(a^{2}b^{-4})^{2}} = \frac{a^{-3}b^{6}}{a^{4}b^{-8}}$ $= a^{-3-4}b^{6-(-8)}$ $= a^{-7}b^{14}$ $= \frac{b^{17}}{a^{7}}$	$\frac{(w^{-4}v^{5})^{2}}{w^{7}v^{-4}} = \frac{w^{-8}v^{10}}{w^{7}v^{-4}}$ $= w^{(-8)-7}v^{10-(-4)}$ $= w^{-15}v^{14}$ $= \frac{v^{14}}{w^{15}}$	$\frac{d^{-5}e^{6}}{(d^{4}e^{-3})^{2}} = \frac{d^{-5}e^{6}}{d^{8}e^{-6}}$ $= d^{-5-8}e^{6-(-6)}$ $= d^{-13}e^{12}$ $= \frac{e^{12}}{d^{13}}$