

**MATHEMATICS: INDICES** 

Learning Objective: Multiplication, division and negative index laws.

## Index Law for further powers: **Example:** $\left(\frac{a}{b}\right)^m$ $a^m$ Simplify $(a^m)^n = a^{m \times n}$ $(a \times b)^m = a^m \times b^m$ $=\frac{a}{b^m}$ Raise any coefficient to the power outside grouping symbols Keep the same base • Multiply the indices .

| (n³)³ | (3d) <sup>4</sup> | $\left(\frac{3b^3}{7d^5}\right)^2$ | $\left(\frac{5g^3}{4h^7}\right)^3$ |
|-------|-------------------|------------------------------------|------------------------------------|
|       |                   |                                    |                                    |
|       |                   |                                    |                                    |
|       |                   |                                    |                                    |
|       |                   |                                    |                                    |

Simplify the following, giving answers without negative indices.

| $\frac{(x^{-4}y^{3})^{4}}{x^{2}y^{-3}}$ | <u>a<sup>-2</sup>b<sup>5</sup></u><br>(a <sup>3</sup> b <sup>-5</sup> ) <sup>3</sup> | $\frac{(w^{-8}v^2)^3}{w^3v^{-4}}$ | <u>d⁻<sup>6</sup>e<sup>8</sup></u><br>(d <sup>5</sup> e⁻²) <sup>5</sup> |
|---|--|-----------------------------------|---|
|   |  |                                   |   |
|   |  |                                   |   |
|   |  |                                   |   |
|   |  |                                   |   |



## MATHEMATICS: ANSWER SHEET

**Learning Objective:** Multiplication, division and negative index laws.

## Index Law for further powers:Example: $(a^m)^n = a^{m \times n}$ $(a \times b)^m = a^m \times b^m$ $(\frac{a}{b})^m = \frac{a^m}{b^m}$ $\cdot$ Raise any coefficient to the power outside<br/>grouping symbolsSimplify $\cdot$ Keep the same base $(a^4)^3 = a^{4 \times 3}$ $(5k)^2 = 5^2k^2$ $(\frac{2x^3}{y^5})^6 = \frac{2^{1 \times 6}x^{3 \times 6}}{y^{5 \times 6}}$ $\cdot$ Multiply the indices

## Simplify the following questions.

| (n <sup>3</sup> ) <sup>3</sup>  | (3d) <sup>4</sup>   | $\left(\frac{3b^3}{7d^5}\right)^2$   | $\left(\frac{5g^3}{4h^7}\right)^3$   |
|---|---|--|--|
| (n <sup>3</sup> ) <sup>3</sup> = n <sup>3×3</sup><br>= n <sup>9</sup> | (3d) <sup>4</sup> = 3 <sup>4</sup> x d <sup>4</sup><br>= 81d <sup>4</sup> | $\left(\frac{3b^{3}}{7d^{5}}\right)^{2} = \frac{3^{2}b^{3\times2}}{7^{2}d^{5\times2}}$ $= \frac{9b^{6}}{49d^{10}}$ | $\left(\frac{5g^3}{4h^7}\right)^3 = \frac{5^3g^{3\times 3}}{4^3h^{7\times 3}}$ $= \frac{125g^9}{64h^{21}}$ |

Simplify the following, giving answers without negative indices.

| $\frac{(x^{-4}y^{3})^{4}}{x^{2}y^{-3}}$  | <u>a<sup>-2</sup>b<sup>5</sup></u><br>(a <sup>3</sup> b <sup>-5</sup> ) <sup>3</sup>               | $\frac{(w^{-8}v^2)^3}{w^3v^{-4}}$  | <u>d<sup>-6</sup>e<sup>8</sup></u><br>(d <sup>5</sup> e <sup>-2</sup> ) <sup>5</sup>                 |
|--|--|--|--|
| $\frac{(x^{-4}y^{3})^{4}}{x^{2}y^{-3}} = \frac{x^{-16}y^{12}}{x^{2}y^{-3}}$ $= x^{-16-2}y^{12-(-3)}$ | $\frac{a^{-2}b^5}{(a^3b^{-5})^3} = \frac{a^{-2}b^5}{a^9b^{-15}}$ $= a^{-2}b^{-9}b^{-5}b^{-5}(-15)$ | $\frac{(W^{-8}V^2)^3}{W^3V^{-4}} = \frac{W^{-24}V^6}{W^3V^{-4}}$ $= W^{(-24)-3}V^{6-(-4)}$ | $\frac{d^{-6}e^{8}}{(d^{5}e^{-2})^{5}} = \frac{d^{-6}e^{8}}{d^{25}e^{-10}}$ $= d^{-6-25}e^{8-(-10)}$ |
| = x <sup>-18</sup> y <sup>15</sup><br>v <sup>15</sup>  | $= a^{-7}b^{20} \\ = \frac{b^{20}}{a^{7}}$   | $= w^{-27} v^{10}$ $= \frac{v^{10}}{w^{27}}$   | $= d^{-31} e^{18}$ $= \frac{e^{18}}{d^{31}}$   |
| $= \frac{y^{15}}{x^{18}} \\ = \frac{y^5}{x^6}$   | a <sup>7</sup>   | W <sup>27</sup>  | a  |